



# Economic Dispatch and Unit Commitment of a Single Micro-Gas Turbine under CHP Operation



Johannes F. Rist

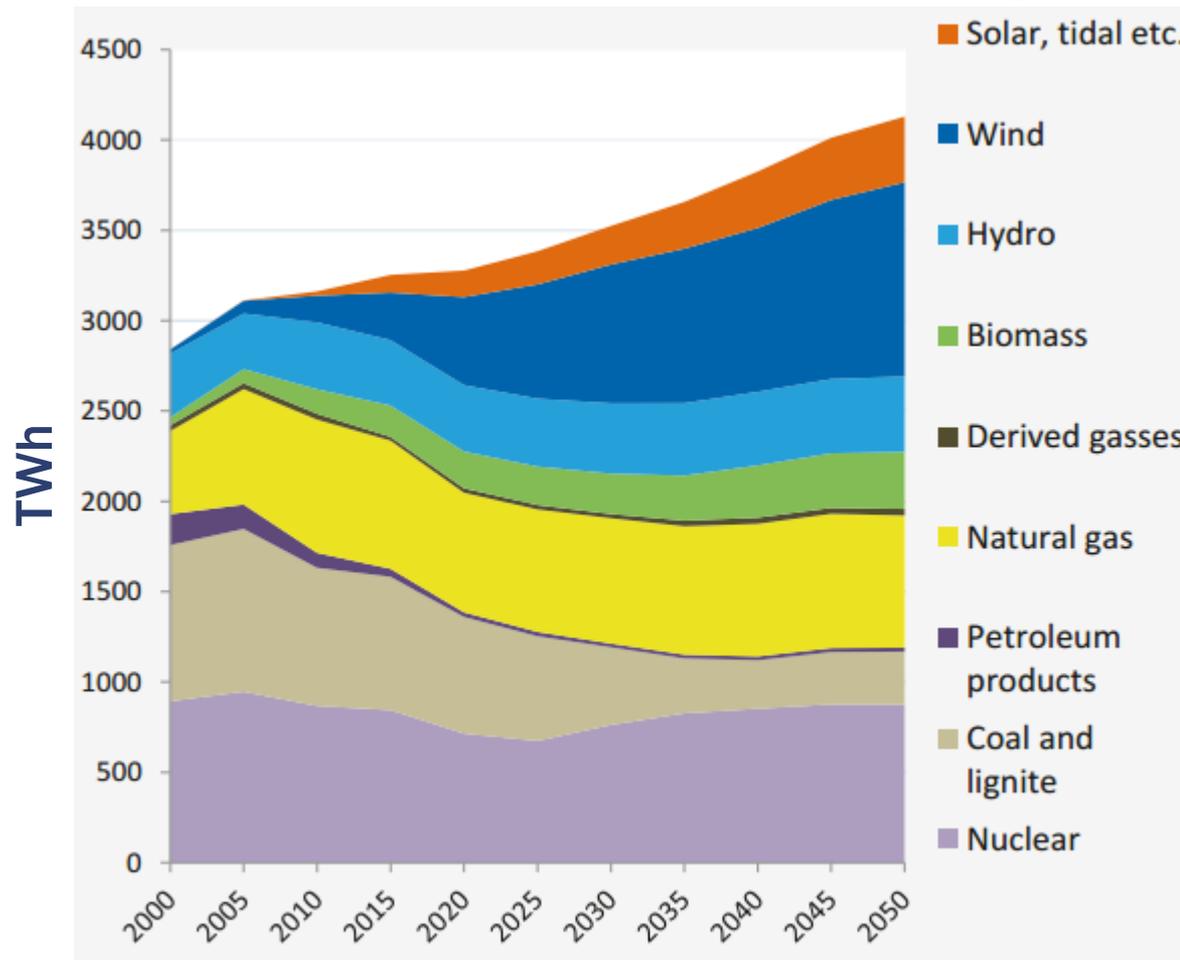
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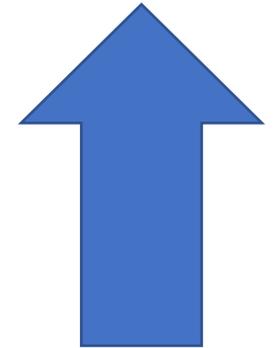
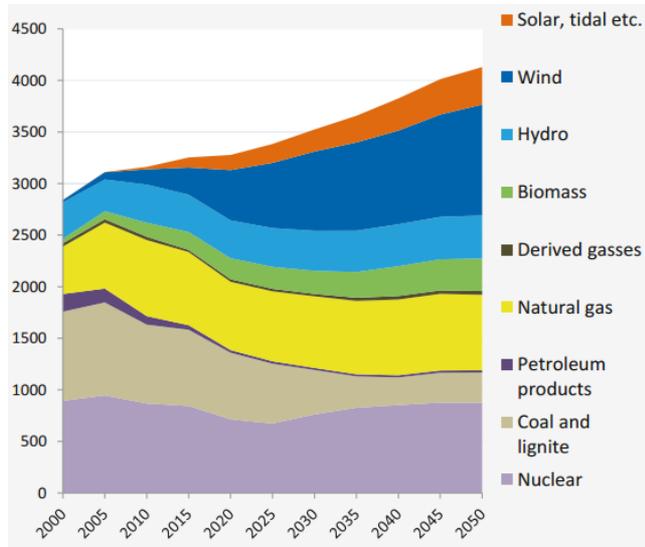
# The Future Energy Landscape



## EU electricity generation trends

(taken from “EU Energy, Transmission, and GHG Emissions: Trends to 2050 – Reference Scenario 2013”)

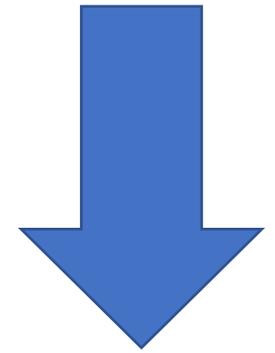
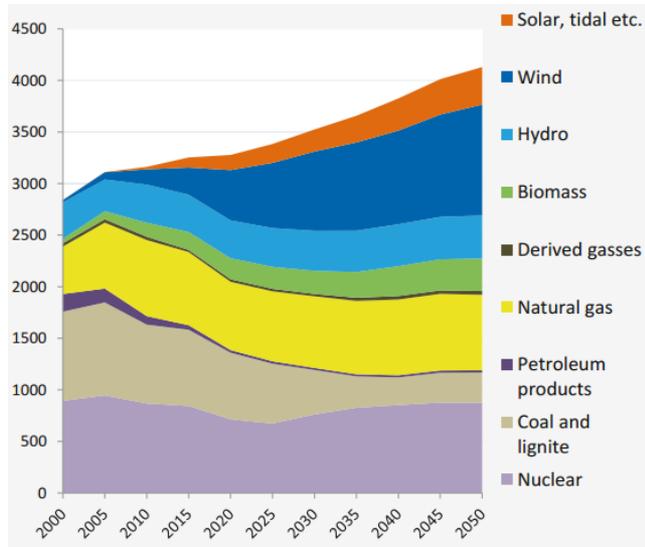
# The Future Energy Landscape



Increasing integration  
Into the grid!

...intermittent and not  
on demand!

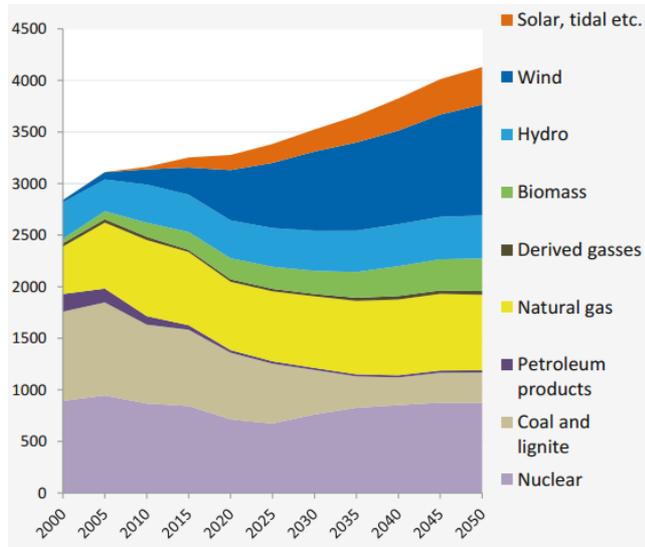
# The Future Energy Landscape



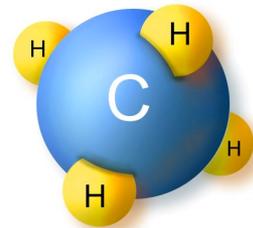
environmental  
concerns

finite resource

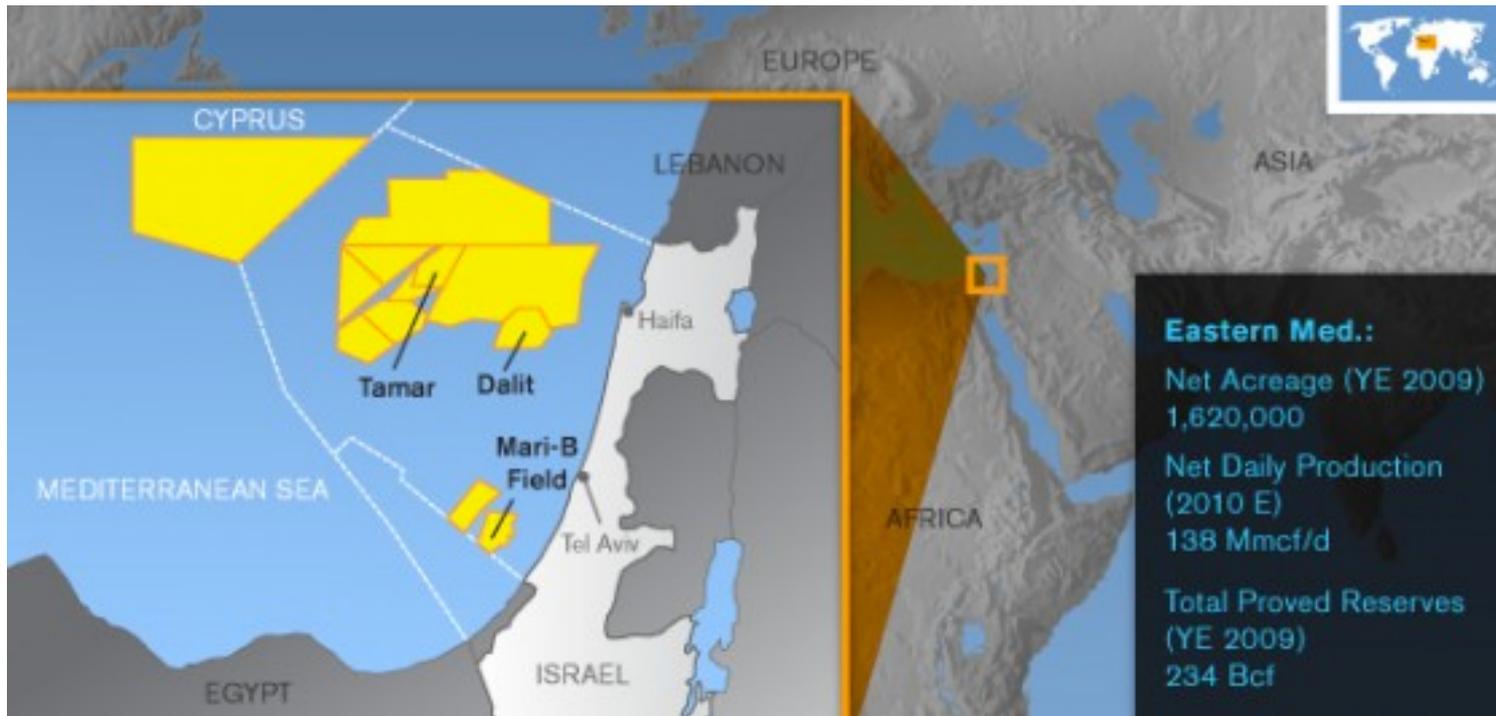
# The Future Energy Landscape



**Natural Gas** is  
clean, cheap, and  
safe!



# Energy Independence in Israel



source: <https://www.greenprophet.com/2012/02/israel-lebanon-natural-gas-discovery/>

**Leviathan** - 22 trillion cubic feet

**Tamar** – 10.8 trillion cubic feet

**Tanin** - 3 trillion cubic feet

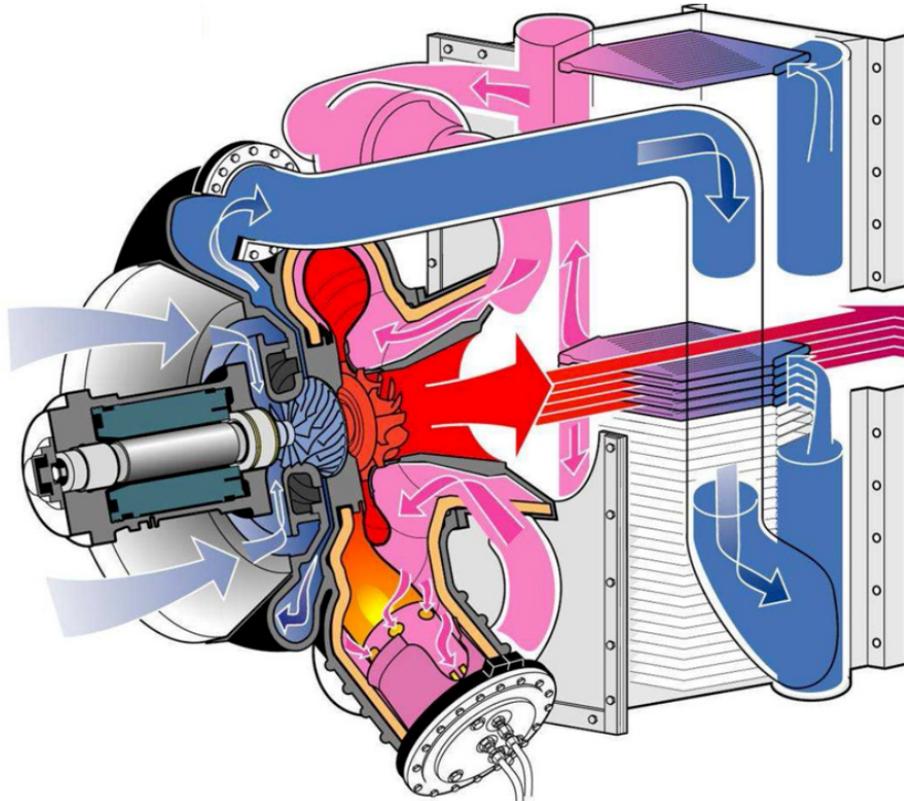
**Natural Gas could transform  
Israel's energy market!**

# Natural Gas and the Smart Grid



Natural gas is the *ideal* near-term solution to bridge the gap between traditional energy generation and renewables

# Micro-Gas Turbines for CHP

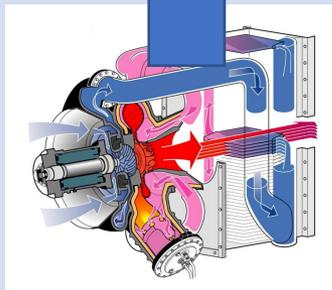


- runs on natural gas
- high power-to-weight ratio
- small terrain footprint
- reliable (few moving parts)
- quiet
- **agile and flexible – on-demand!**

**Electricity and Heating/Cooling Generation**

# MGT Integration into the Grid

consumer



MGT

utility



Meet the consumer power demand  
in an economically optimal way

# The Economic Dispatch Problem

**Economic Dispatch** is a short-term scheduling for the output of a number of electricity generation facilities required to **meet system demand** at the **lowest cost** subject to **operational constraints**

$$\min \quad J(P, H) \quad \text{\$}$$

$$s.t. \quad P = D_P$$

$$H = D_H$$

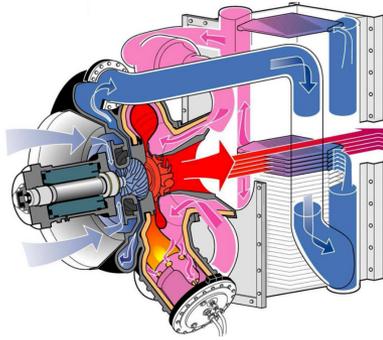
**Power Balance**

operational constraints

$D_P$  **Electricity Demand**

$D_H$  **Heat Demand**

# The Economic Dispatch Problem



## What is the cost of operating an MGT?

- relation of fuel consumption to heat and power output
- start-up and shut-down costs
- time constants for power delivery



## Electricity and Heat Tariffs

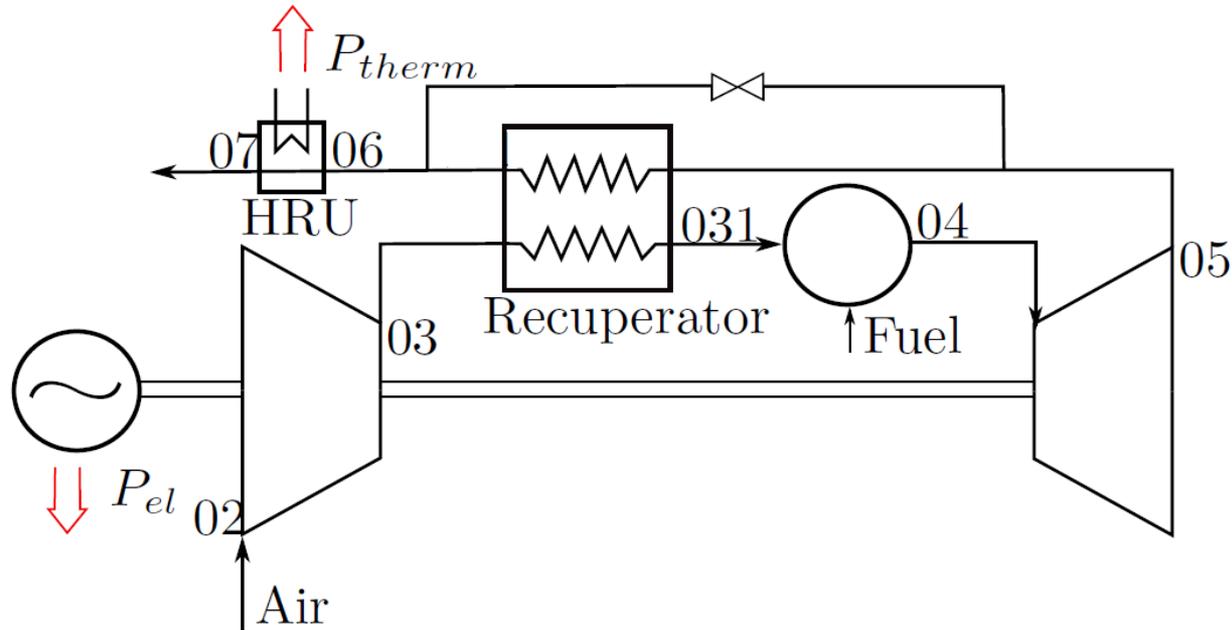
- how much does electricity cost
- electricity market for buying and selling power



## Consumer Needs

- what are the power and heat demand profiles for consumers

## Recuperated Gas Turbine Cycle Diagram

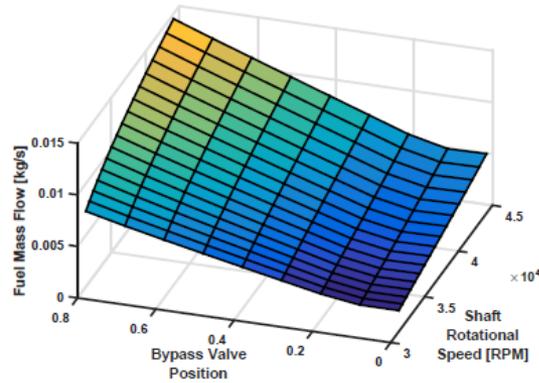


- 02 – 03 : **Compressor** – flow pressure rises.
- 03 – 031 : **Recuperator** – the temperature of the flow is further increased in the recuperator by energy recovering.
- 031 – 04 : **Combustor** – energy addition.

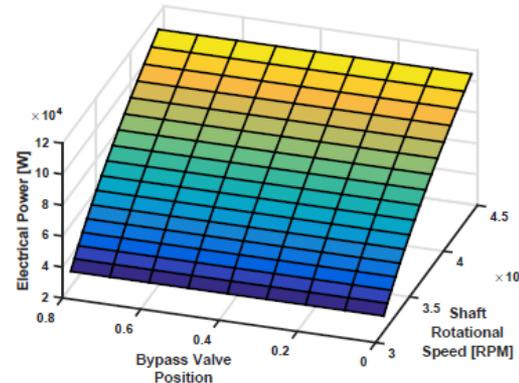
- 04 – 05 : **Turbine** – the thermal energy is converted into mechanical energy that is provided to compressor and the electrical power generator.



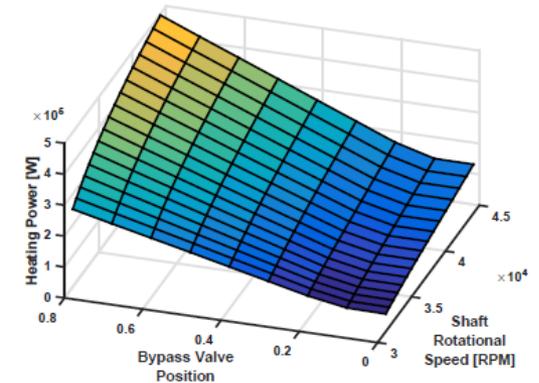
# MGT Modeling



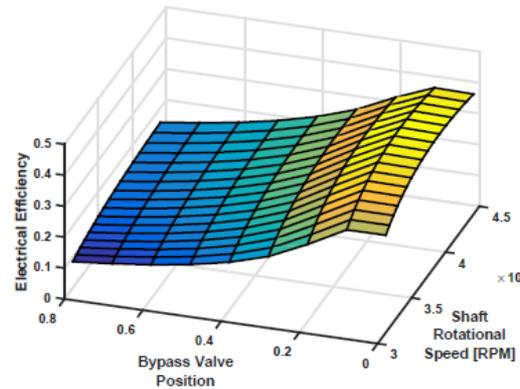
(a) Fuel Mass Flow.



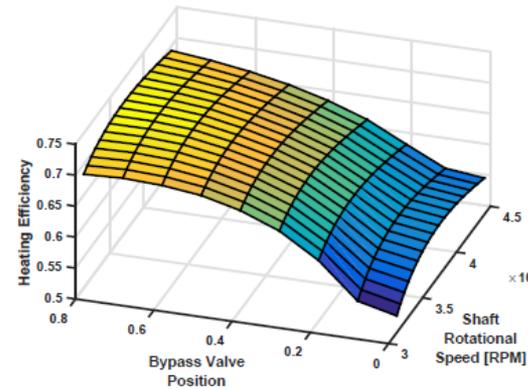
(b) Electricity Output.



(c) Heat output.



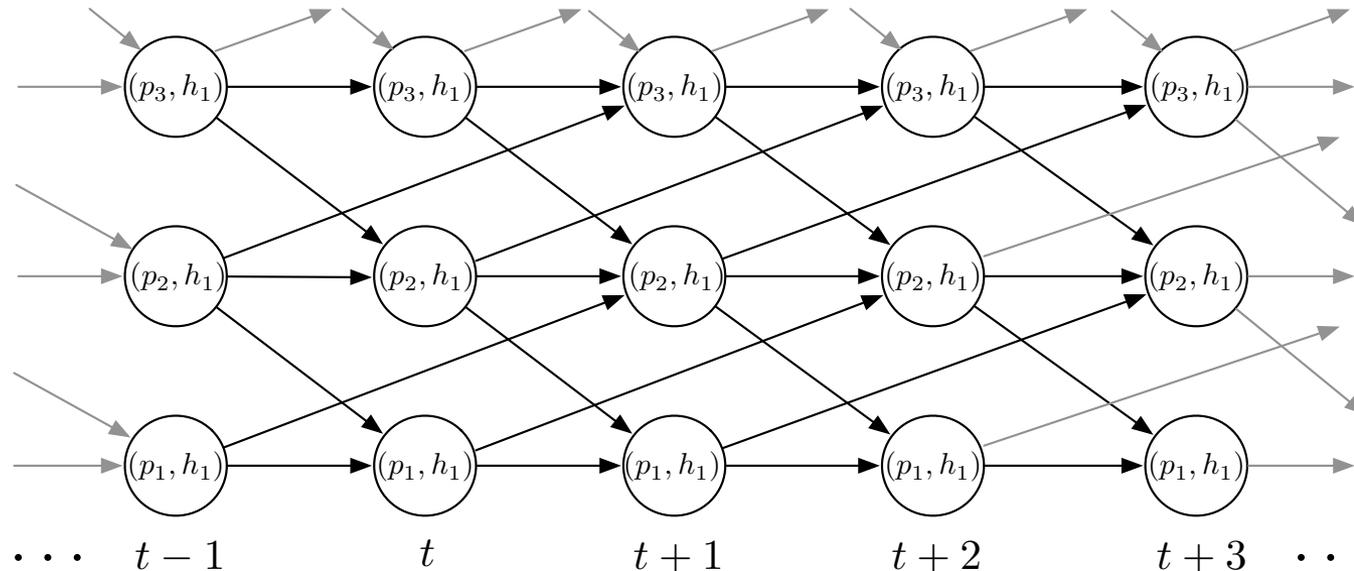
(d) Electrical Efficiency.



(e) Heat Efficiency.

# Towards an Optimization Model

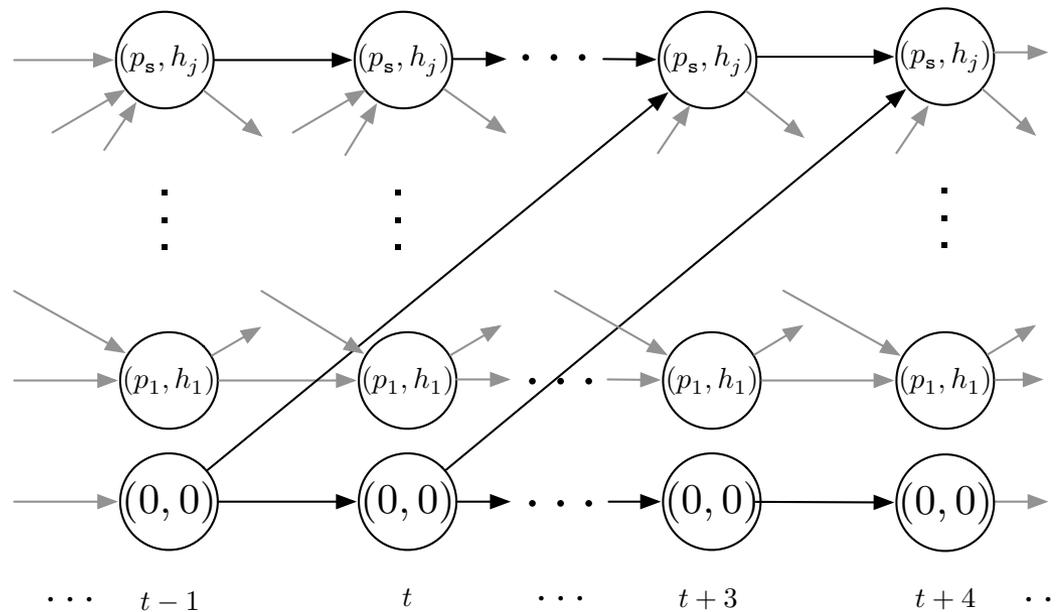
## Operational Constraints as discretized state-transition graph



- system “state” is shaft speed and bypass valve
- arrows indicate allowable transitions to new steady-states, and their time

# Towards an Optimization Model

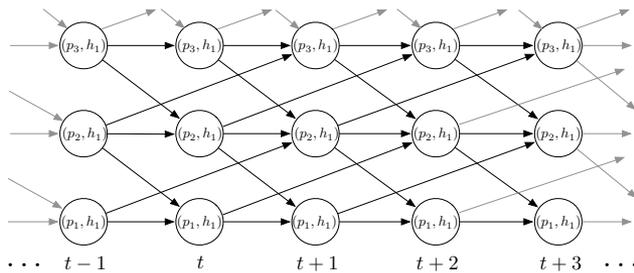
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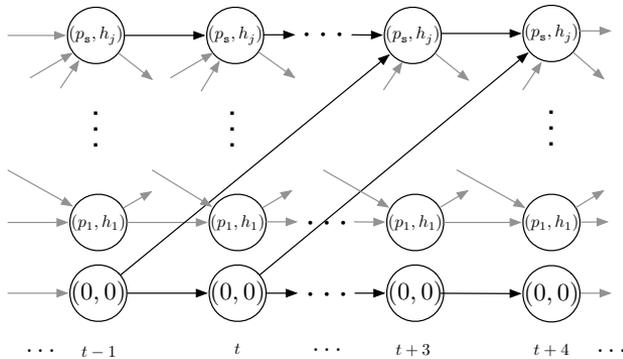
# Towards an Optimization Model

## Operational Constraints as discretized state-transition graph



MGT Dynamics can be represented by graphs

$$x_{GT}(t + c\Delta T) = f_{GT}(x_{GT}(t), u_{GT}(t))$$



\$\$ Costs can be assigned to each edge

- relates to fuel price
- maintenance cost
- utility commitment and consumer demand

$$\min_{x_{GT}, u_{GT}, x_{UT}^P, x_{UT}^H} J(x_{GT}, u_{GT}, x_{UT}^P, x_{UT}^H)$$

subject to

(MGT Dynamics)  $x_{GT}(t + c\Delta T) = f_{GT}(x_{GT}(t), u_{GT}(t)),$

(Power Balance)  $P_{GT}(x_{GT}(t)) + (x_{UT}^P(t) - P(t)) = 0,$

(Heat Balance)  $H_{GT}(x_{GT}(t)) + (x_{UT}^H(t) - H(t)) = 0,$

$$x_{GT}(t) \in \{(p_i(t), h_j(t)), i = 1, \dots, \mathbf{s}, j = 1, \dots, \mathbf{v}\}$$

$$x_{UT}^P(t) \geq 0, x_{UT}^H(t) \geq 0, t = 1, \dots, T.$$

**Optimization over a *directed acyclic graph***

**Shortest Path Algorithm** – complexity is linear in #nodes+edges

# Case Studies



## Full Service Restaurant

commercial medium electricity tariff

$511m^2$

Demand and Tariff Data

US DOE 2004



## Large Hotel

commercial tall electricity tariff

$11,345m^2$



## Small Hotel

commercial medium electricity tariff

$4,013m^2$

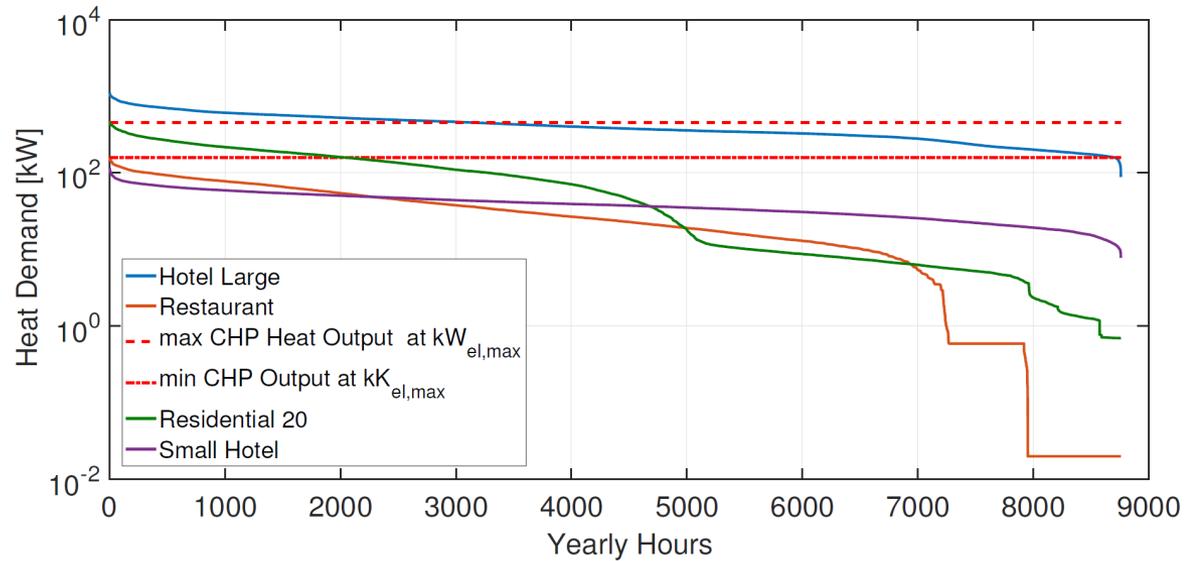
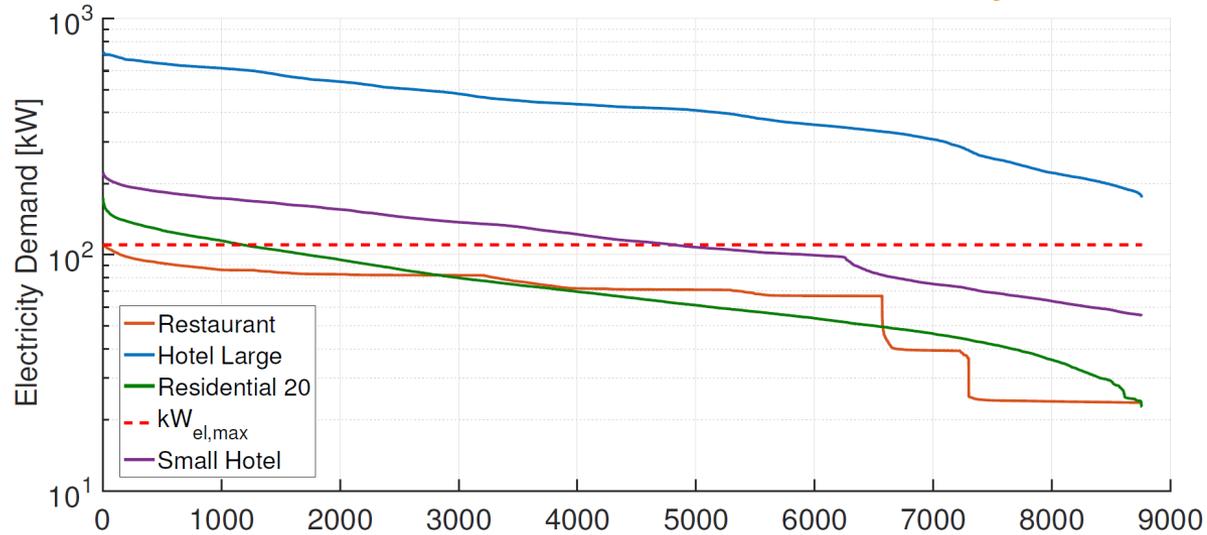


## Residential Building

residential electricity tariff

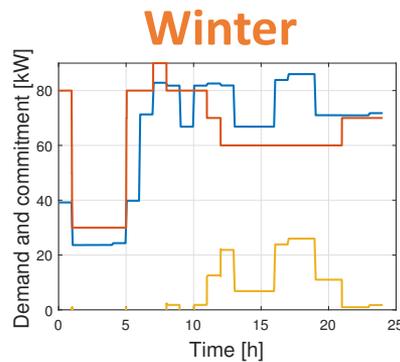
neighborhood of 20 apartment buildings

# Case Studies

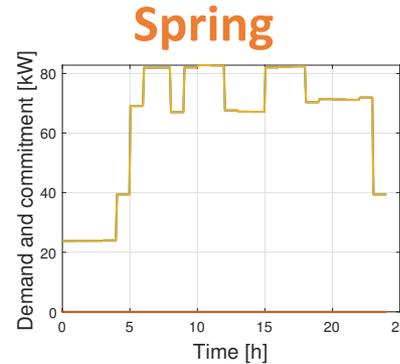


# Full Service Restaraunt

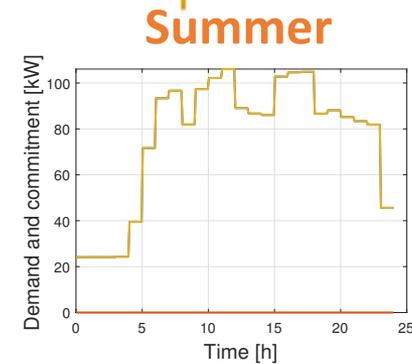
## Power



(a) Power Demand: Reference Winter Day

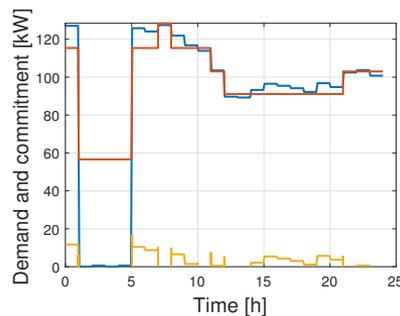


(b) Power Demand: Reference Spring Day

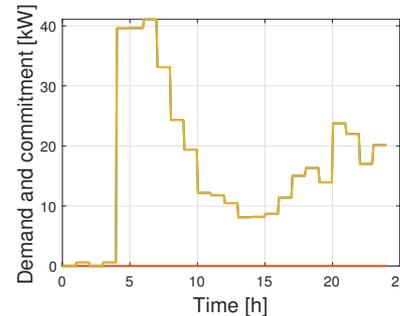


(c) Power Demand: Reference Summer Day

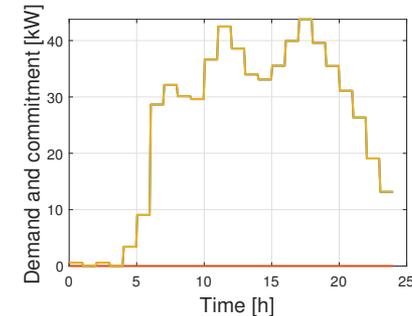
## Heat



(d) Heat Demand: Reference Winter Day



(e) Heat Demand: Reference Spring Day



(f) Heat Demand: Reference Summer Day



## Heat Driven Operation

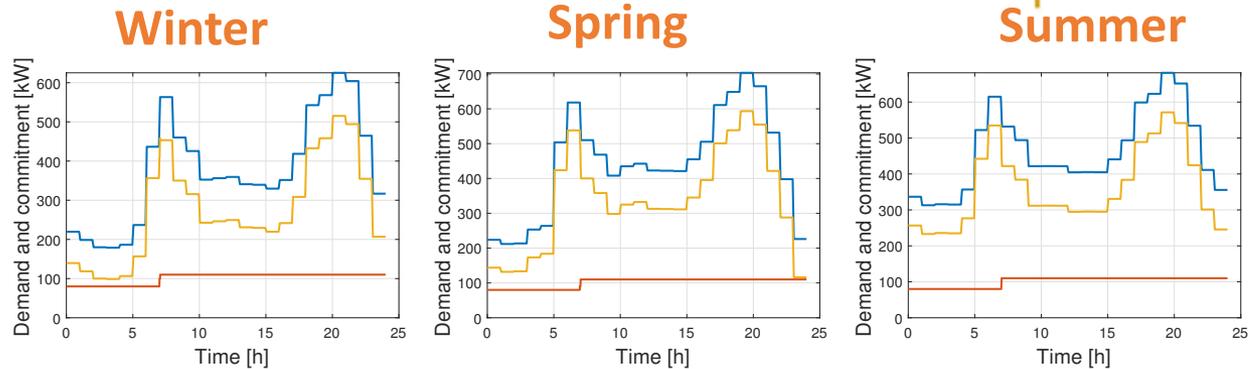
During winter, electricity is a byproduct of meeting the heat demand.

## Maintenance Driven Operation

In Summer and Spring, startup and shutdown costs are too high to operate the MGT.

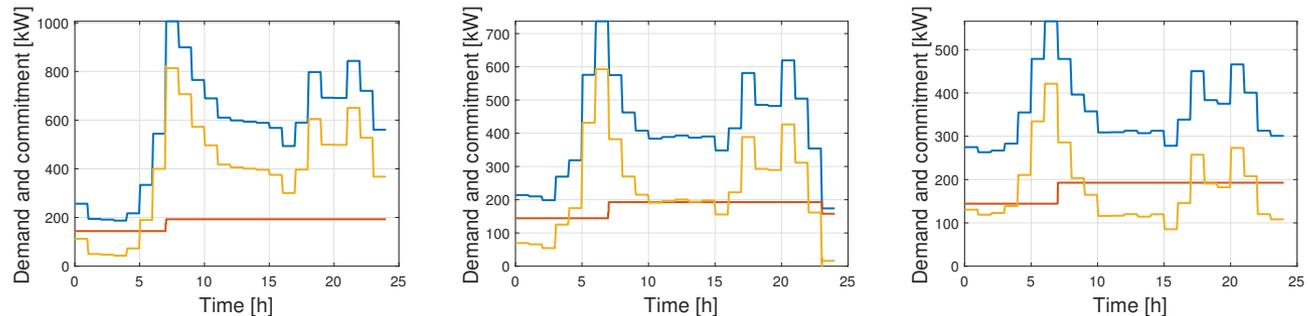
# Large Hotel

## Power

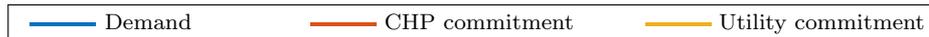


(a) Power Demand: Reference Winter Day (b) Power Demand: Reference Spring Day (c) Power Demand: Reference Summer Day

## Heat



(d) Heat Demand: Reference Winter Day (e) Heat Demand: Reference Spring Day (f) Heat Demand: Reference Summer Day



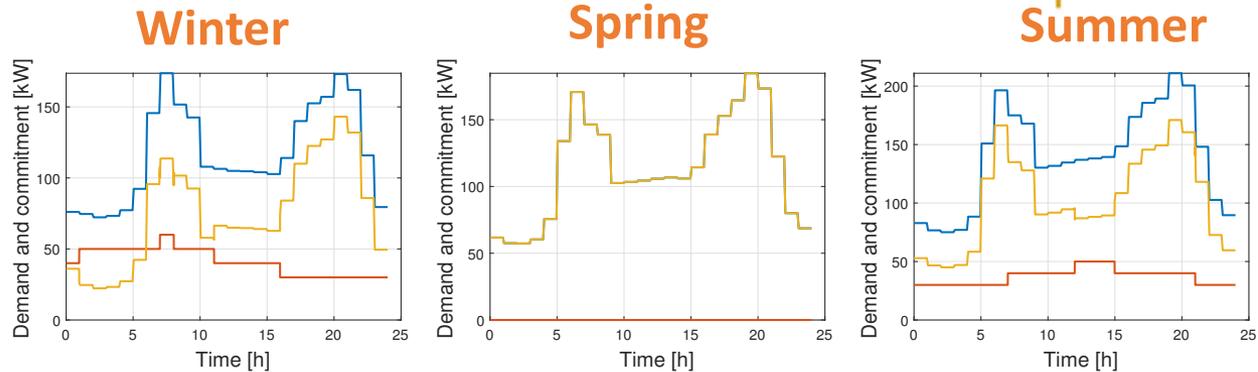
## Electricity Driven Operation

Power demand of the large hotel exceeds the maximum capacity of the MGT.

Optimal commitment requires contributions from both MGT and Utility

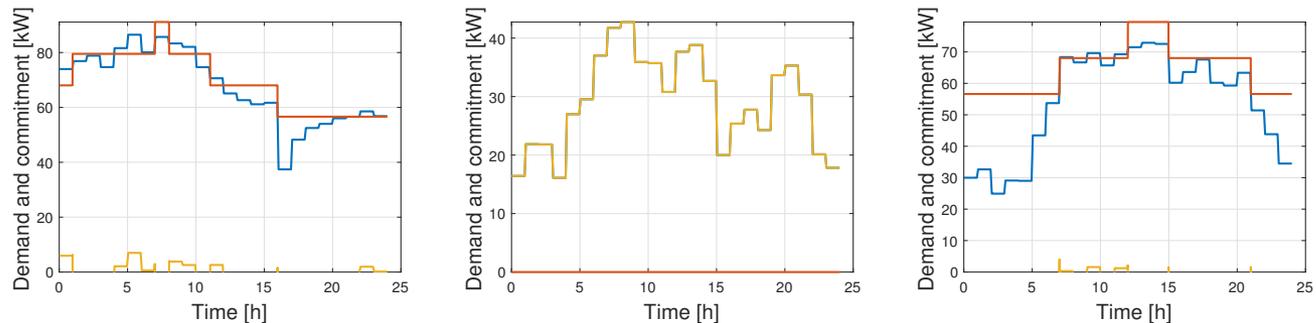
# Small Hotel

## Power



(a) Power Demand: Reference Winter Day (b) Power Demand: Reference Spring Day (c) Power Demand: Reference Summer Day

## Heat



(d) Heat Demand: Reference Winter Day (e) Heat Demand: Reference Spring Day (f) Heat Demand: Reference Summer Day

## Heat Driven Operation

MGT operates at low power commitment levels, while heat demand is supplied at a competitive unit efficiency

## Maintenance Driven Operation

During off-peak hours in summer, the MGT is operated to avoid additional startup/shutdown costs

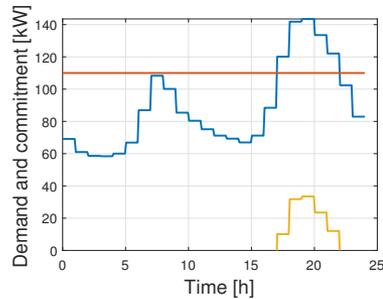
# Residential Community

Winter

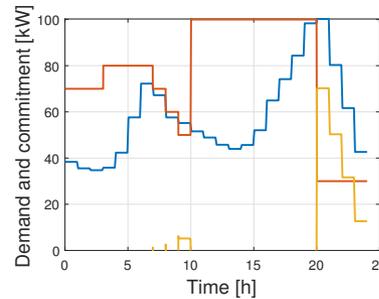
Spring

Summer

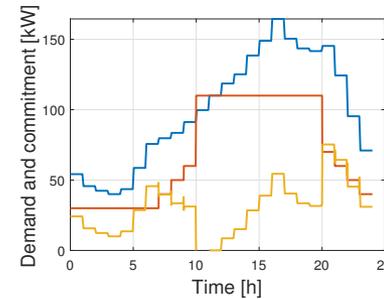
Power



(a) Power Demand: Reference Winter Day

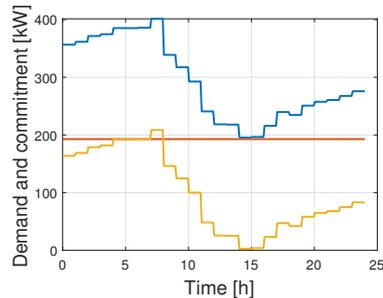


(b) Power Demand: Reference Spring Day

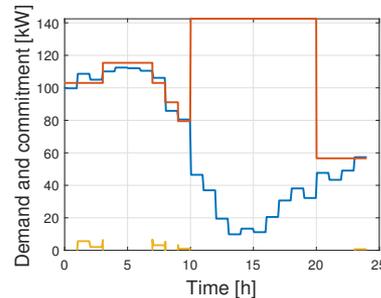


(c) Power Demand: Reference Summer Day

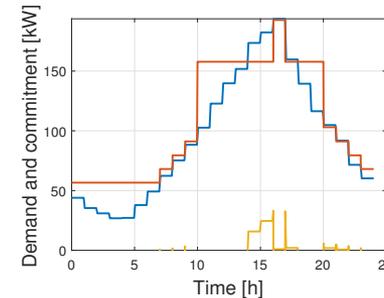
Heat



(d) Heat Demand Reference Winter Day



(e) Heat Demand: Reference Spring Day



(f) Heat Demand: Reference Summer Day



## Revenue Driven Operation

In intermediate tariff hours, the MGT operates above the demand, selling electricity back to the grid

## Flexible Operations

During off-peak hours, the MGT either operates **electricity, heat, or maintenance** driven, depending on situation

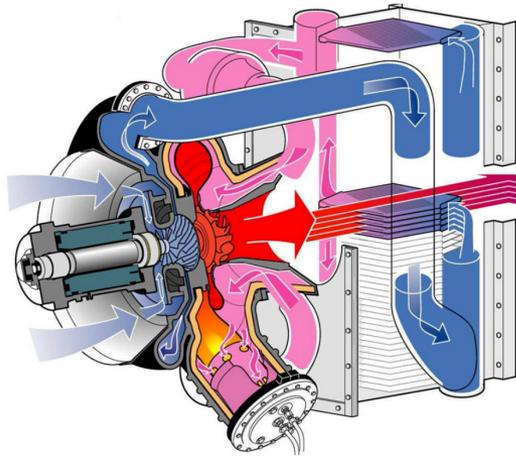
**Electricity Driven:** In case of the large hotel, when power and heat demand exceed the MGT capability permanently.

**Heat Driven:** Small hotel and restaurant due to more competitive energy generation with respect to the demand profiles.

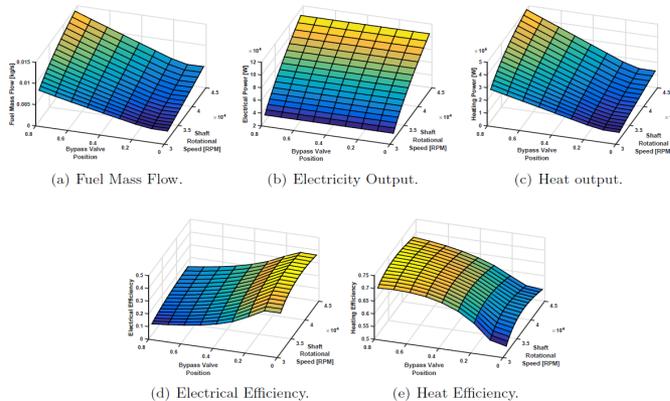
**Maintenance Driven:** In off-peak hours of the small hotel and restaurant where utility prices are low to avoid cycle costs.

**Revenue Driven:** Operation in residential neighbourhood aims to generate excess electricity that can be sold to the grid.

# Conclusions



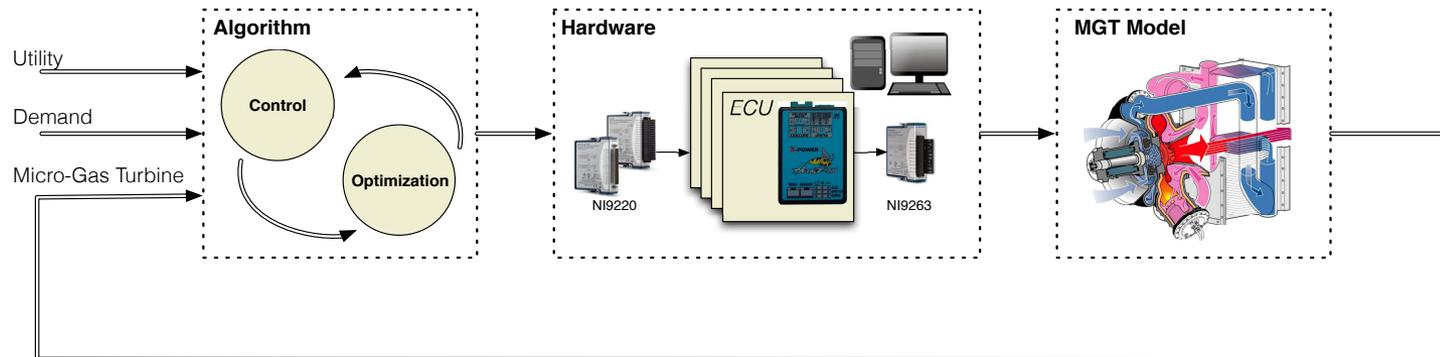
Micro-Gas Turbines using natural gas is an economically viable solution towards a distributed power generation economy



Detailed modeling required to gain a better understanding of the economic operational modes of the MGT

a dynamic real-time algorithm for integration of the MGT into the smart-grid

operation of MGT “banks” for distributed economic dispatch



# Acknowledgements



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Technion



MAX-PLANCK-GESELLSCHAFT

*Economic Dispatch and Unit Commitment of a Single Micro-Gas Turbine under CHP Operation, Applied Energy (under review).*

## Questions?